

$$2a) \hat{p} = \frac{4}{26} = 0.153846154$$

$$\hat{q} = 0.846153846$$

$$2b) \hat{R} = \frac{65}{104} = 0.625 = \frac{\bar{y}}{\bar{x}}$$

$$1 - \hat{R} = 0.375$$

$$2c) \hat{\mu}_{Y_d} = \bar{d} + \mu_x$$

$$\bar{d} = \bar{y} - \bar{x}$$

$$\mu_x = \frac{\sum x_i}{N} = \frac{3040}{800} = 3.8 = \mu_x$$

$$\bar{y} = \frac{65}{26} = 2.5, \quad \bar{x} = \frac{104}{26} = 4$$

$$\hat{\mu}_{Y_d} = (2.5 - 4) + 3.8$$

$$\hat{\mu}_{Y_d} = 2.3$$

$$T_d = (800)(2.3)$$

$$T_d = 1840$$

$$2d) \hat{\mu}_{y_g} = \hat{R} \mu_x = \frac{\bar{y}}{\bar{x}} \mu_x \quad \begin{array}{l} (x: \text{nb. de personnes}) \\ (y: \text{nb. de visites}) \end{array}$$

$$\mu_x = \frac{3040}{800} = 3.8$$

$$\bar{y} = 26/26 = 1, \quad \bar{x} = \frac{104}{26} = 4$$

$$\hat{\mu}_{y_g} = \left(\frac{1}{4.0}\right)(3.8)$$

$$\hat{\mu}_{y_g} = 0.95$$

$$T_g = (800)(0.95)$$

$$T_g = 760$$

$$2e) \hat{p} = 0.153846$$

$$\hat{\sigma}_{\hat{p}} = \sqrt{\frac{(0.153846)(0.846153)}{26-1}} \sqrt{1 - \frac{26}{800}}$$

$$= 0.072160170 * 0.983615$$

$$= 0.0709778$$

Aut. 2006

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2f)

$$\hat{R} = 0.625, \hat{R}^2 = 0.4225$$

$$\hat{R} = \frac{\text{nb. def.}}{\text{nb. de personnes}}$$

$$\hat{\sigma}_{\hat{R}} = \frac{\sqrt{1 - \frac{n}{N}}}{\sqrt{n}} \sqrt{\frac{\Delta y^2 + \hat{R}^2 \Delta x^2 - 2\hat{R}\Delta x\Delta y}{\bar{x}}}$$

$$= \frac{\sqrt{1 - \frac{26}{800}}}{\sqrt{26}} \sqrt{\frac{3.06 + (0.4225)(2.88) - 2 * 0.625 * 2.06}{4.0}}$$

$$= 0.048225693 \sqrt{1.0268}$$

$$= \quad \quad * 1.013311403$$

$$= 0.0488676$$

29)

$$\bar{T}_d = N \hat{\mu}_{y_d}$$

$$= N [\bar{d} + \mu_x]$$

$$\hat{\sigma}_{\bar{T}_d} = N \hat{\sigma}_{\hat{\mu}_{y_d}}$$

$$= N \frac{\sqrt{1 - \frac{n}{N}}}{\sqrt{m}} \sqrt{s_y^2 + s_x^2 - 2s_{xy}}$$

$$= 800 \frac{\sqrt{1 - \frac{26}{800}}}{\sqrt{26}} \sqrt{3.06 + 2.88 - 2 * 2.6}$$

$$= 154.3222 * 0.860232527$$

$$= 132.75299$$

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$$\begin{aligned}
 a) \quad m_0 &= \left( \frac{2 \Delta y}{R \bar{y}} \right)^2 \\
 &= \left( \frac{2 * 1.749285}{(0.10)(2.5)} \right)^2 \\
 &= 195.83987
 \end{aligned}$$

$$m = \frac{m_0}{1 + \frac{m_0}{N}} \quad N = 800$$

$$m = 157.32639$$

$$\begin{aligned}
 3b) \quad \hat{R} &= \frac{65/26}{3040/800} = \frac{2.5}{3.8} = \frac{\bar{y}}{\mu_x} \\
 \hat{R} &= 0.6578
 \end{aligned}$$

$$\begin{aligned}
 3c) \quad \hat{\sigma}_{\hat{R}} &= \frac{1}{\mu_x} \frac{\Delta y}{\sqrt{n}} \sqrt{1 - \frac{n}{N}} \\
 &= \left( \frac{1}{3.8} \right) \left( \frac{1.749285}{\sqrt{26}} \right) \sqrt{1 - \frac{26}{800}} \\
 \hat{\sigma}_{\hat{R}} &= 0.08880
 \end{aligned}$$

$$3d) \quad \bar{y}' = \frac{3 + 2 + 2 + 1 + 22(0)}{26}$$

$$\bar{y}' = 0.30769$$

$$s_{y'} = 0.788377$$

$$T' = N \bar{y}'$$

$$= 800 * 0.30769$$

$$T' = 246.15384$$

$$3e) \quad T' = N \bar{y}'$$

$$\hat{\sigma}_{T'} = N \frac{s_{y'}}{\sqrt{26}} \sqrt{1 - \frac{26}{800}}$$

$$= 800 * \frac{0.788377}{\sqrt{26}} \sqrt{1 - \frac{26}{800}}$$

$$\hat{\sigma}_{T'} = 121.66408$$